

Chapter 1

① a. $2(x+3)(x-3) + 1)^2$

$$2(x^2 - 9 + 1)^2$$

$$2(x^2 - 8)^2 = 2(x^2 - 8)(x^2 - 8)$$

$$2(x^4 - 16x^2 + 64) = \boxed{2x^4 - 32x^2 + 128}$$

b. $g(x) = x^2 - 9$

$$f(x) = (x+1)(x+1) = (x^2 + 2x + 1)^2 = 2x^2 + 4x + 2$$

$$g(f(x)) = \boxed{(2x^2 + 4x + 2)^2 - 9}$$

expand if you want

c. $((c^2+1)+3)((c^2+1)-3)$

$$(c^2+4)(c^2-2) = \boxed{c^4 + 2c^2 - 8}$$

d. $k(x) = x+1$

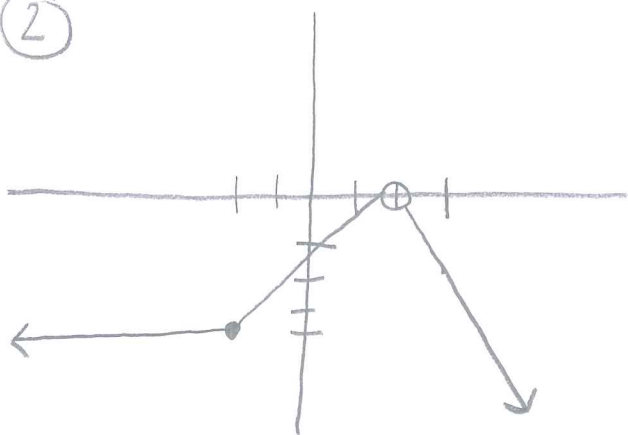
$$h(x) = 2x^2$$

Other answers possible

e. $(-\infty, \infty)$

f. no. one-to-one means it passes the horizontal line test.

②



Chapter 2

1. a. $f(x) = x^2 + 2x - 35$

$$y = x^2 + 2x - 35$$

$$y + 35 = x^2 + 2x$$

$$y + 35 + \frac{1}{4} = x^2 + 2x + \frac{1}{4}$$

$$y + 36 = (x+1)^2$$

$$y = (x+1)^2 - 36$$

$$v. = (-1, -36)$$

minimum value

$$\text{Zeros: } (x+7)(x-5)$$

$$(-7, 0)(x+5)$$

b. $f(x) = 4x^2 - 8x - 1$

$y = 4x^2 - 8x - 1$

$y + 1 = 4x^2 - 8x$

$y + 1 + \underline{\hspace{2cm}} = 4x^2 - 8x + \underline{\hspace{2cm}}$

$y + 1 + \underline{4} = 4(x^2 - 2x + \underline{1})$

$y + 5 = 4(x - 1)^2$

$y = 4(x - 1)^2 - 5$

Vertex = (1, -5)

minimum

Zeros: $0 = 4(x - 1)^2 - 5$

$5 = 4(x - 1)^2$

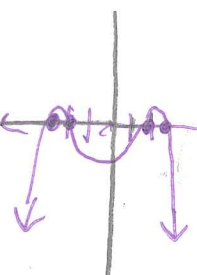
$\frac{5}{4} = (x - 1)^2$

$\pm \sqrt{\frac{5}{4}} + 1 = x \quad \left(\frac{\sqrt{5}}{2} + 1, 0\right)$

$\pm \frac{\sqrt{5}}{2} + 1 = x \quad \left(-\frac{\sqrt{5}}{2} + 1, 0\right)$

2. $F(x) = -x^4 + 9x^2 - 20$
 $-(x^4 - 9x^2 + 20)$

$-(x^2 - 5)(x^2 - 4)$



Zero @
 $(-\sqrt{5}, 0)$
 $(\sqrt{5}, 0)$
 $(2, 0)$
 $(-2, 0)$

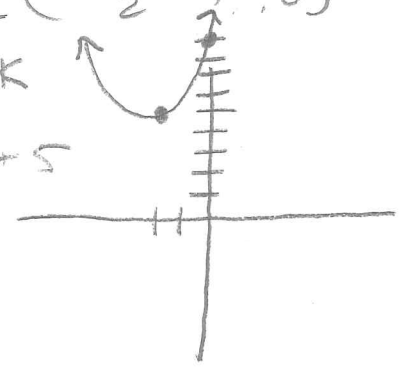
3. $y = a(x - h)^2 + k$

$9 = a(0 + 2)^2 + 5$

$9 = a(4) + 5$

$9 = 4a + 5$

$4 = 4a, a = 1$



4.

	x^3	$5x^2$	$-8x$	19
x^4	x^4	$5x^3$	$-8x^2$	$19x$
$7x^3$	$2x^3$	$10x^2$	$-16x$	38
		$2x^2$	$3x$	14

$= \boxed{x^3 + 5x^2 - 8x + 19 + \frac{-24}{x+2}}$

Standard/vertex form = $y = (x + 2)^2 + 5$

Quadratic form: $(x + 2)(x + 2) + 5$
 $x^2 + 4x + 4 + 5$

NO x-intercepts $y = x^2 + 4x + 9$

5. $\frac{(x - 6)(x + 3)(x + 2)(x - 1)}{(x - 2)(x + 2)(x - 1)}$

7. $(x + 1)(x - 1)(x + 2i)(x - 2i)$
 multiply out

6. $g, f(x) = \frac{4+i}{4-i} \cdot \frac{4+i}{4+i} = \frac{16 + 8i - 1}{16 - i^2}$
 $= \frac{15 + 8i}{17} = \frac{15}{17} + \frac{8i}{17}$

h. $\frac{5}{1+i} - \frac{3i}{1-i}$

$\frac{5(1-i)}{(1+i)(1-i)} - \frac{3i(1+i)}{(1-i)(1+i)} = \frac{5 - 5i - 3i - 3i^2}{2}$
 $= \frac{5 - 8i + 3}{2} = \frac{8 - 8i}{2}$
 $= \boxed{4 - 4i}$

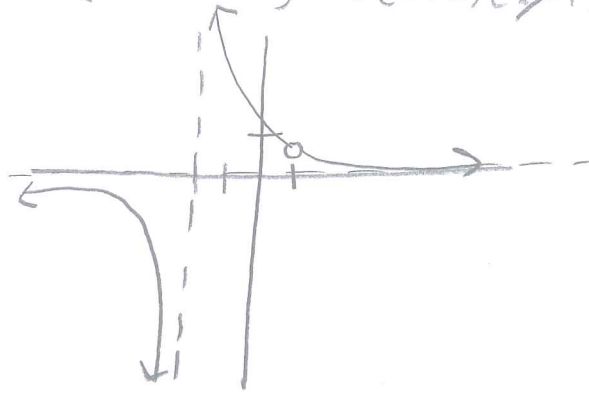
$$8. f(x) = \frac{3x-3}{2x^2+2x-4} = \frac{3(x-1)}{2(x^2+x-2)} = \frac{3(x-1)}{2(x+2)(x-1)} = \frac{3}{2(x+2)}$$

H.A @ $y=0$

V.A @ $x=-2$

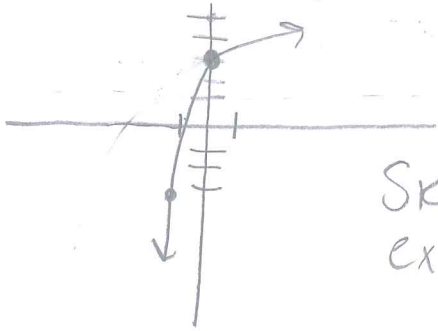
Hole @ $(1, \frac{1}{2})$

$$\frac{3}{2(1+2)} = \frac{3}{2(3)} = \frac{3}{6} = \frac{1}{2}$$



Chapter 3

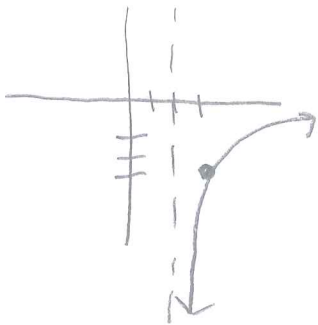
1. a. $f(x) = 4 - e^{-2x} = -e^{-2x} + 4$



e^x has point @ $(0, 1)$
and H.A. @ $y=0$

SKIP, you won't have to graph this on exam.

b. $f(x) = \log_3(x-2) - 3$



2. 1. $\log_5 x + 2 \log_5 w$

2. $\log_2 \frac{\sqrt{x} u}{z^5 y^3}$

3. $\log_{1/3} 27$

$$\frac{1}{3}^x = 27$$

$$x = -3$$

4. $\log_4 256 = 4$

5. $3 = \frac{x-2}{x}$

$$3x = x - 2 \quad x = -1$$

$2x = -2$ Extraneous
So no value exists.

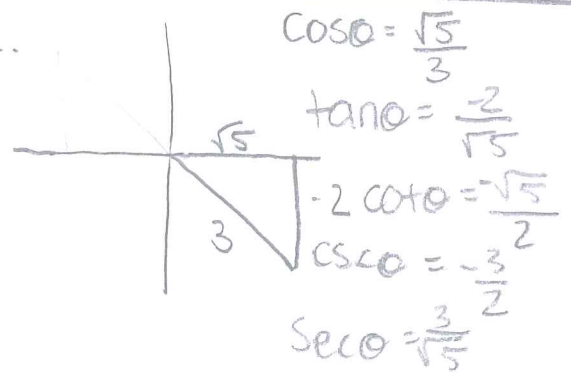
Chapter 4

1. $\frac{-25\pi}{12} + \frac{24\pi}{12} = \frac{-\pi}{12} + \frac{24\pi}{12} = \frac{23\pi}{12}$

Keep adding until positive

$$\begin{aligned} (-2)^2 + b^2 &= 3^2 \\ 4 + b^2 &= 9 \quad b^2 = 5 \\ b &= \sqrt{5} \end{aligned}$$

2.



$$3. \begin{array}{|c|c|} \hline \rightarrow & Q3 \\ \hline \star & \star \\ \hline \end{array} \quad \left| \quad 4. \frac{\pi}{3} \right.$$

Chapter 7

$$1. \begin{bmatrix} 4 & 0 & -4 \\ 4 & -3 & -1 \end{bmatrix} \cdot \begin{bmatrix} 0 \\ 25 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ -75 \end{bmatrix}$$

$$2 \times 3 \quad 3 \times 1$$

$$2. ad - bc = -8 - (-15) = 7$$

$$3. ad - bc = 72 - 81 = -9$$

$$\frac{1}{-9} \begin{bmatrix} 8 & -9 \\ -9 & 9 \end{bmatrix} = \begin{bmatrix} -\frac{8}{9} & 1 \\ 1 & -1 \end{bmatrix}$$