Related Rates Extra Practice

Solve each related rate problem.

1) A hypothetical cube shrinks so that the length of its sides are decreasing at a rate of 4 m/min. At what rate is the volume of the cube changing when the sides are 8 m each?

2) A hypothetical square grows so that the length of its diagonals are increasing at a rate of 5 m/min. How fast is the area of the square increasing when the diagonals are 11 m each?

3) A conical paper cup is 10 cm tall with a radius of 10 cm. The cup is being filled with water so that the water level rises at a rate of 4 cm/sec. At what rate is water being poured into the cup when the water level is 2 cm?

4) A hypothetical cube grows at a rate of 27 m³/min. How fast are the sides of the cube increasing when the sides are 7 m each?

5) A hypothetical square shrinks at a rate of 9 m²/min. At what rate are the sides of the square changing when the sides are 12 m each?

6) A conical paper cup is 20 cm tall with a radius of 10 cm. The bottom of the cup is punctured so that the water leaks out at a rate of $\frac{9\pi}{4}$ cm³/sec. At what rate is the water level changing when the water level is 7 cm?

7) A spherical balloon is deflated at a rate of 36π cm³/sec. At what rate is the radius of the balloon changing when the radius is 9 cm?

8) Oil spilling from a ruptured tanker spreads in a circle on the surface of the ocean. The area of the spill increases at a rate of 81π m²/min. How fast is the radius of the spill increasing when the radius is 15 m?

9) A spherical balloon is deflated at a rate of $\frac{36\pi}{V}$ cm³/sec, where V is the volume of the balloon. At what rate is the radius of the balloon changing when the radius is 2 cm?

10) A hypothetical square grows at a rate of $8 \text{ m}^2/\text{min}$. How fast are the diagonals of the square increasing when the diagonals are 10 m each?

Related Rates Extra Practice

Name

Solve each related rate problem.

1) A hypothetical cube shrinks so that the length of its sides are decreasing at a rate of 4 m/min. At what rate is the volume of the cube changing when the sides are 8 m each?

 $V = \text{volume of cube} \quad s = \text{length of sides} \quad t = \text{time}$ Equation: $V = s^3$ Given rate: $\frac{ds}{dt} = -4$ Find: $\frac{dV}{dt}\Big|_{s=8}$ $\frac{dV}{dt}\Big|_{s=8} = 3s^2 \cdot \frac{ds}{dt} = -768 \text{ m}^3/\text{min}$

2) A hypothetical square grows so that the length of its diagonals are increasing at a rate of 5 m/min. How fast is the area of the square increasing when the diagonals are 11 m each?

A = area of square
$$x = \text{length of diagonals}$$
 $t = \text{time}$
Equation: $A = \frac{x^2}{2}$ Given rate: $\frac{dx}{dt} = 5$ Find: $\frac{dA}{dt}\Big|_{x = 11}$
 $\frac{dA}{dt}\Big|_{x = 11} = x \cdot \frac{dx}{dt} = 55 \text{ m}^2/\text{min}$

3) A conical paper cup is 10 cm tall with a radius of 10 cm. The cup is being filled with water so that the water level rises at a rate of 4 cm/sec. At what rate is water being poured into the cup when the water level is 2 cm?

$$V = \text{volume of material in cone} \quad h = \text{height} \quad t = \text{time}$$

Equation: $V = \frac{\pi h^3}{3}$ Given rate: $\frac{dh}{dt} = 4$ Find: $\frac{dV}{dt}\Big|_{h=2}$
 $\frac{dV}{dt}\Big|_{h=2} = \pi h^2 \cdot \frac{dh}{dt} = 16\pi \text{ cm}^3/\text{sec}$

4) A hypothetical cube grows at a rate of 27 m³/min. How fast are the sides of the cube increasing when the sides are 7 m each?

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V = \text{volume of cube} \quad s = \text{length of sides} \quad t = \text{time}
Equation: V = s^3 Given rate: \frac{dV}{dt} = 27 Find: \frac{ds}{dt}\Big|_{s=7}
\frac{ds}{dt}\Big|_{s=7} = \frac{1}{3s^2} \cdot \frac{dV}{dt} = \frac{9}{49} m/min
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5) A hypothetical square shrinks at a rate of $9 \text{ m}^2/\text{min}$. At what rate are the sides of the square changing when the sides are 12 m each?

$$A = \text{area of square} \quad s = \text{length of sides} \quad t = \text{time}$$

Equation: $A = s^2$ Given rate: $\frac{dA}{dt} = -9$ Find: $\frac{ds}{dt}\Big|_{s=12}$
 $\frac{ds}{dt}\Big|_{s=12} = \frac{1}{2s} \cdot \frac{dA}{dt} = -\frac{3}{8} \text{ m/min}$

6) A conical paper cup is 20 cm tall with a radius of 10 cm. The bottom of the cup is punctured so that the water leaks out at a rate of $\frac{9\pi}{4}$ cm³/sec. At what rate is the water level changing when the water level is 7 cm?

$$V = \text{volume of material in cone} \quad h = \text{height} \quad t = \text{time}$$

Equation: $V = \frac{\pi h^3}{12}$ Given rate: $\frac{dV}{dt} = -\frac{9\pi}{4}$ Find: $\frac{dh}{dt}\Big|_{h=7}$
 $\frac{dh}{dt}\Big|_{h=7} = \frac{4}{\pi h^2} \cdot \frac{dV}{dt} = -\frac{9}{49}$ cm/sec

7) A spherical balloon is deflated at a rate of 36π cm³/sec. At what rate is the radius of the balloon changing when the radius is 9 cm?

$$V = \text{volume of sphere } r = \text{radius } t = \text{time}$$

Equation: $V = \frac{4}{3}\pi r^3$ Given rate: $\frac{dV}{dt} = -36\pi$ Find: $\frac{dr}{dt}\Big|_{r=9}$
 $\frac{dr}{dt}\Big|_{r=9} = \frac{1}{4\pi r^2} \cdot \frac{dV}{dt} = -\frac{1}{9} \text{ cm/sec}$

8) Oil spilling from a ruptured tanker spreads in a circle on the surface of the ocean. The area of the spill increases at a rate of 81π m²/min. How fast is the radius of the spill increasing when the radius is 15 m?

$$A = \text{area of circle} \quad r = \text{radius} \quad t = \text{time}$$

Equation: $A = \pi r^2$ Given rate: $\frac{dA}{dt} = 81\pi$ Find: $\frac{dr}{dt}\Big|_{r=15}$
 $\frac{dr}{dt}\Big|_{r=15} = \frac{1}{2\pi r} \cdot \frac{dA}{dt} = \frac{27}{10}$ m/min

9) A spherical balloon is deflated at a rate of $\frac{36\pi}{V}$ cm³/sec, where V is the volume of the balloon. At what rate is the radius of the balloon changing when the radius is 2 cm?

$$V = \text{volume of sphere} \quad r = \text{radius} \quad t = \text{time}$$

Equation: $V = \frac{4}{3}\pi r^3$ Given rate: $\frac{dV}{dt} = -\frac{36\pi}{V}$ Find: $\frac{dr}{dt}\Big|_{r=2}$
 $\frac{dr}{dt}\Big|_{r=2} = \frac{1}{4\pi r^2} \cdot \frac{dV}{dt} = -\frac{27}{128\pi} \text{ cm/sec}$

10) A hypothetical square grows at a rate of 8 m²/min. How fast are the diagonals of the square increasing when the diagonals are 10 m each?

$$A = \text{area of square} \quad x = \text{length of diagonals} \quad t = \text{time}$$

Equation: $A = \frac{x^2}{2}$ Given rate: $\frac{dA}{dt} = 8$ Find: $\frac{dx}{dt} \Big|_{x=10}$
 $\frac{dx}{dt} \Big|_{x=10} = \frac{1}{x} \cdot \frac{dA}{dt} = \frac{4}{5}$ m/min

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