

## 2016 HONORS PRECALCULUS CHAPTER 6 FREE-RESPONSE QUESTION

### SECTION 1, PART I and II

A graphing calculator is allowed for these problems.

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**Part I:** An airplane is flying directly north at 300 miles/hour. There is a very strong crosswind of 45 miles per hour blowing directly from the west.

- Draw a vector diagram that models this situation.
- If no correction is made for the wind, what is the final bearing of the plane?
- If no correction is made for the wind, what is the final ground speed of the plane?
- What will the plane's coordinates be after 60 minutes? 30 minutes?

**Part II:** Another small plane traveling at 200 miles/hour leaves the origin at the same time as the plane in Part I. It points directly south, and is also subject to the 45 mile/hour crosswind that is blowing directly from the west.

- Draw a vector diagram representing the movements of **both planes**.
- What is the distance between the planes after 30 minutes have passed?
- After 30 minutes have passed, the control tower at  $(0, 0)$  measures the angle between the two planes in degrees. What is the angle they measure?

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#### Part I Solutions

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- Setup  $\rightarrow \tan\theta = \frac{300}{45}$ , bearing =  $8.53^\circ$
- Setup  $\rightarrow \|v\| = \sqrt{45^2 + 300^2}$ , magnitude = 303.36 mph
- 60 minutes  $(45, 300)$ ; 30 minutes  $(22.5, 150)$

#### Part I Points

- 1 point for wind vector  
1 point for airspeed vector  
1 point for accurate vector lengths
- 1 point for setup  
1 point for bearing =  $8.53^\circ$   
1 point for units
- 1 point for setup  
1 point for magnitude = 303.36 mph  
1 point for units
- 1 point for coordinate after 60 minutes  
1 point for coordinate after 30 minutes  
1 point for correct parenthesis
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#### Part II Solutions

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- 250 miles apart
- Setup  $\rightarrow \cos\theta = \frac{\langle 22.5, 150 \rangle \cdot \langle 22.5, -100 \rangle}{(\sqrt{22.5^2 + 150^2})(\sqrt{22.5^2 + 100^2})} = 158.78^\circ$

#### Part II Points

- 1 point for wind vector  
1 point for plane vector #1  
1 point for plane vector #2  
1 point for accurate vector lengths
- 1 point for answer  
1 point for units
- 1 point for setup  
1 point for answer  
1 point for units

